How Can Bayesian Smoothing and Correspondence Analysis Help Decipher the Occupational Histories of Late-eighteenth Century Slave Quarters at Monticello?

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Introduction

Two problems hinder effective intrasite spatial

- 1. Small samples from individual quadrats hide patterns in artifact-type frequencies in a sea of sampling variation.
- 2. The meaning of quadrat groups—created by clustering algorithms on the basis of similarity in type frequencies—often is

In this poster, we build on earlier work (Robertson 1999, Neiman et al. 2000) to explore two promising solutions: Bayesian smoothing and correspondence analysis (CA).

Bayes in Space

Bayes's theorem offers an elegant means to address the sample-size problem. Bayes's theorem shows frequencies likely to occur in a given quadrat, characterized by a "prior" probability distribution, with type frequencies actually found there to produce smoothed estimates that have lower sampling error than the raw counts.



The Bayesian estimates honor, in a statistically defensible fashion, 1) sample size in a given quadrat, 2) mean similarity of a quadrat's type frequencies to the average value for the neighborhood, and 3) mean uncertainty about type frequencies within quadrats in a neighborhood. Bayesian estimates are, therefore, superior to current methods that rely on simple weighted moving averages (e.g., Neiman 1990, Whallon 1984).

Consider the r quadrats that fall within the spatial neighborhood of a given quadrat. Each

vector of sample proportions in the 7th

We suppose that the unknown probabilities, from which all the quadrats in a given sampled from a single, "prior" Dirichlet which we reexpress as $? = \sum \boldsymbol{b}_j$ and a vector of means, $? = \{?_j = \beta_j / K\}$.

Given the Dirichlet prior, with parameters K estimates of the quadrat probabilities the form:



Fienberg and Holland (1972, Bishop et al. 1975) showed that estimates like this have minimum mean-squared error when



estimate the ?, for a spatial neighborhood as the



To estimate the parameter K for a



Correspondence Analysis (CA)

Spatial variation in artifact-type frequencies likely is caused by both temporal and social variation. Common practice in archaeological spatial analysis, based on cluster analysis, confounds these dimensions of variation. CA offers a means to disentangle them.

CA and Frequency Seriation

The frequency-seriation model stipulates that artifact-type frequencies arrayed in time display battleship-shaped, or Gaussian, response curves, provided the requirements of the seriation model are

CA and frequency seriation are intimately related. If type frequencies follow Gaussian response curves with homogeneous variances and assemblages are uniformly distributed in time, the scores of assemblages on the first CA axis approximate maximum-likelihood estimates of their temporal positions. If type frequencies have Gaussian responses to a second, synchronic gradient (orthogonal to time), the assemblage scores on the second CA axis approximate maximum-likelihood Hence, CA is precisely the analytic tool we need to dissect temporal and social gradients underlying spatial variation in type frequencies.



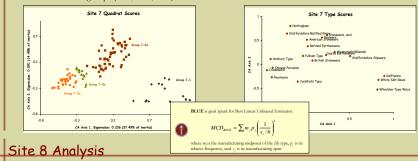
Site Background

Our case study revolves around two adjacent sites on Monticello Mountain, occupied by slaves and an overseer during the second half of the 18th century. We tested the plowzone using a stratified-random sample of 5-foot quadrats, followed by more intensive plowzone sampling adjacent to quadrats with high artifact densities or features. For more see Bon-Harper and Wheeler (2005).



We computed Bayesian estimates of type frequencies in each 5-foot quadrat using neighborhoods with a 40-foot radius. CA suggests there are two major groups of assemblages (7-1, 7-2), the second of which was further divided into three subgroups (7-2a, 7-2b, 7-2c).

Site 7 Analysis

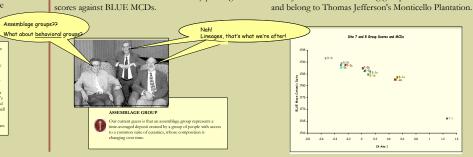


The CA of Site 8 assemblages produced a point scatter in The type scores again indicate time runs from left to right the shape of a sideways Y. We assigned the assemblages along Axis 1. However, here there are unlikely to be cost to three major groups, one in each arm of the Y (8-1, 8-2, differences among the types associated with Axis 2. 8-3), and then split each group in two (a, b).



Synthesis

How do the assemblage groups relate to one another in time and social space? Temporal relationships among them are summarized AND confirmed by plotting Axis-1 scores against BLUE MCDs.



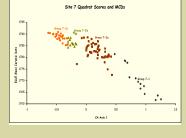
The type scores indicate that Axis 1 captures time, with early types on the right and late types on the left. Axis 2 may represent synchronic variation in cost, with cheaper

Group 7-1 is much earlier than the others. It represents

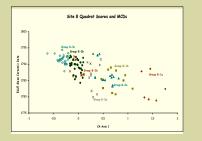
the mid-18th century occupation by slaves belonging to

Peter Jefferson. The remaining groups date c. 1770-1800

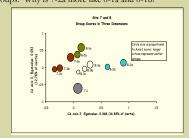




As at Site 7, the correlation between the BLUE MCDs and Axis-1 scores confirms that the latter captures time



There are two additional significant dimensions of variation among the assemblage groups, captured by Axis-2 and Axis-3 scores. With the exception of 7-2a, the subgroups display historical continuity within major groups. Why is 7-2a more like 8-1a and 8-1b?



Discussion

If the grouped assemblages are sorted on their Axis-1 scores, the type frequencies roughly approximate the Gaussian response curves of the CA and frequency-



result of different positions along synchronic dimension of ceramic-ware abundance, especially at Site 8. Might assemblage groups represent residential groups?

In plotting the physical locations of assemblage groups, we see that 7-1 corresponds with a rock chimney base of the mid-18th century slave dwelling, whereas 7-2b and 7-2c match the location of the overseer's house (c. 1770-1800). We wonder if 7-2a represents a group of slaves to the south of the overseer. The affinities between 7-2a, 8-1a, and 8-1b support this idea and indicate the group moved from Site 7 to Site 8. Thereafter, two additional residential groups were established at Site 8, 8-2 and 8-3, while deposition represented by 8-1 ended. By the end of the Site 8 occupation, only 8-3 remained.

